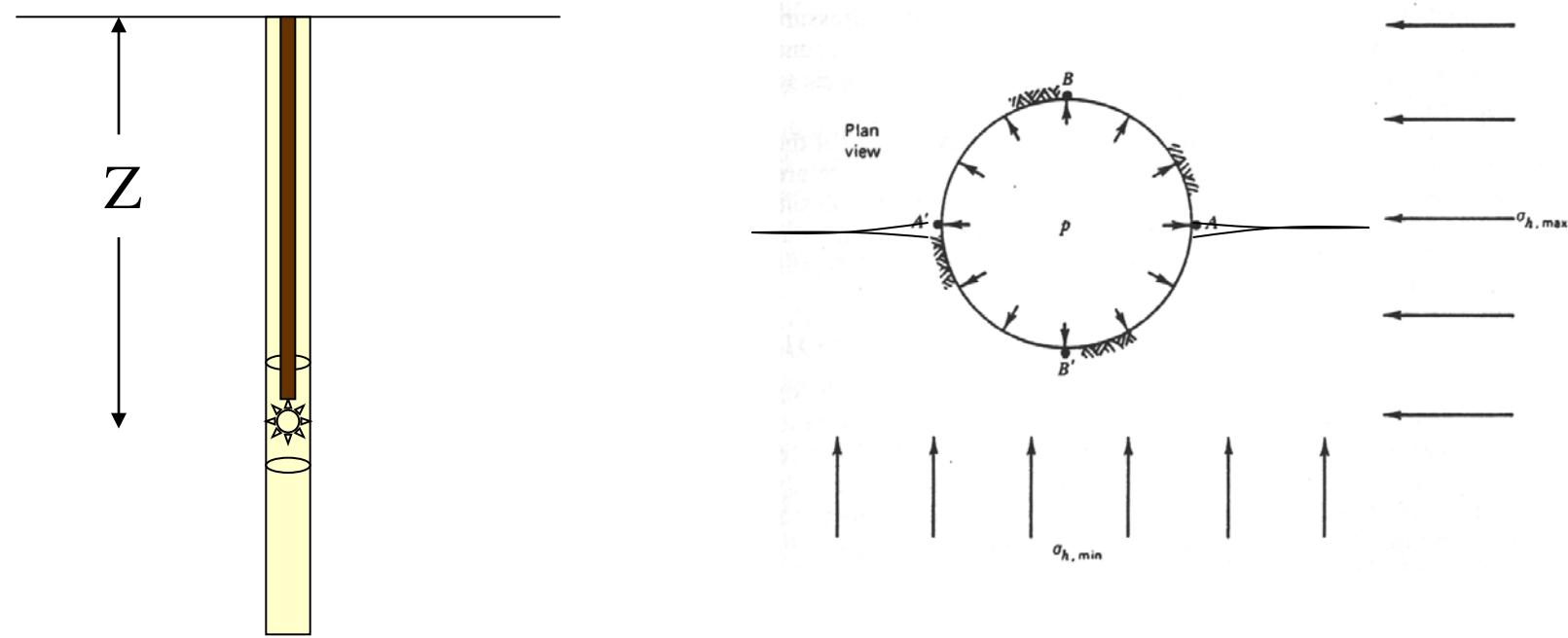
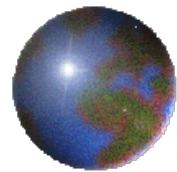


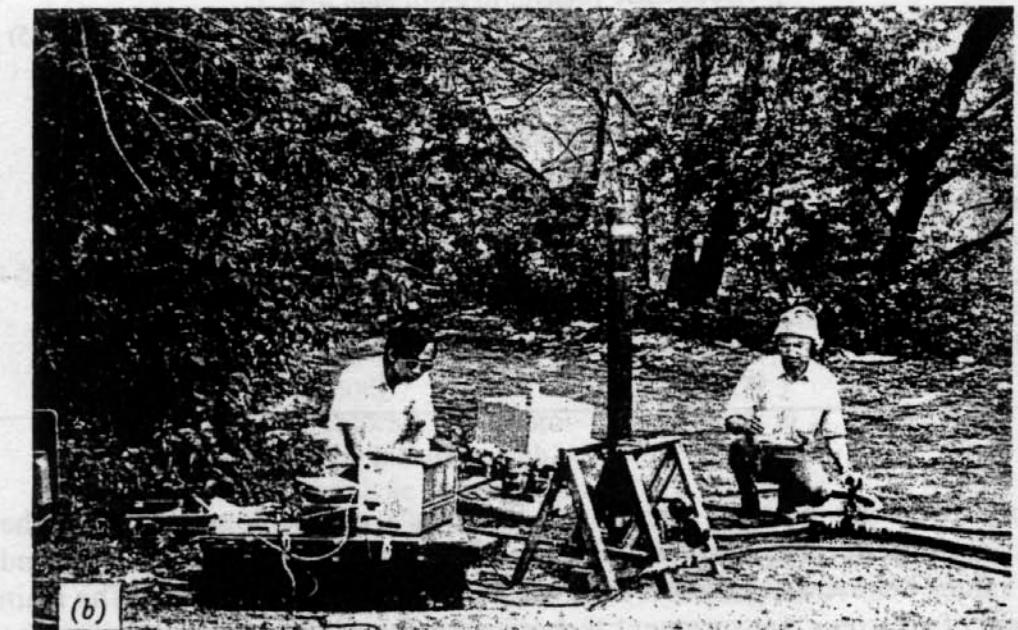
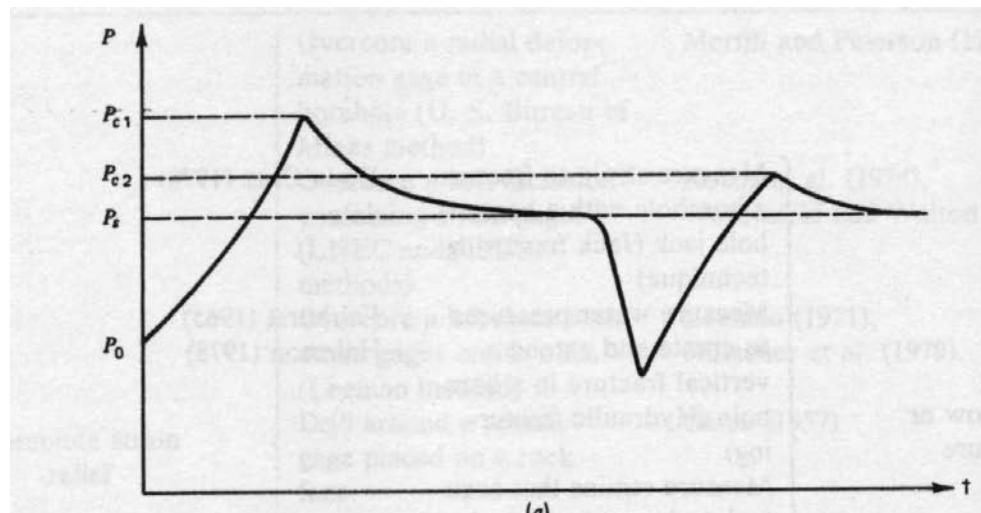
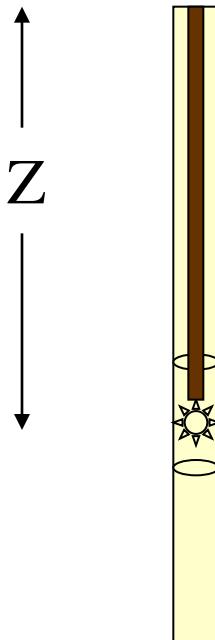
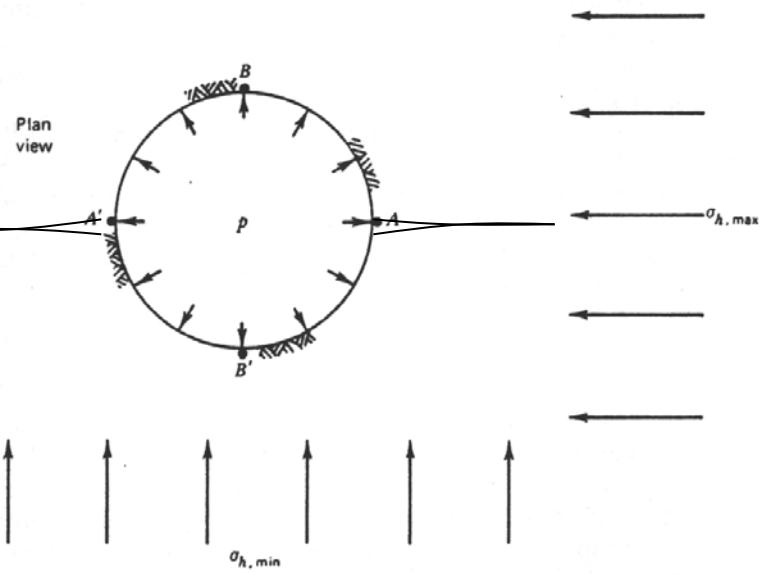
How to measure ?

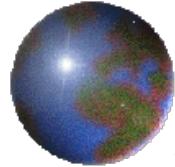
- ➊ Hydraulic method (measure stress at failure)
 - ▣ Hydraulic fracture
 - ▣ Sleeve fracture
 - ▣ Hydraulic test on pre-existing fracture





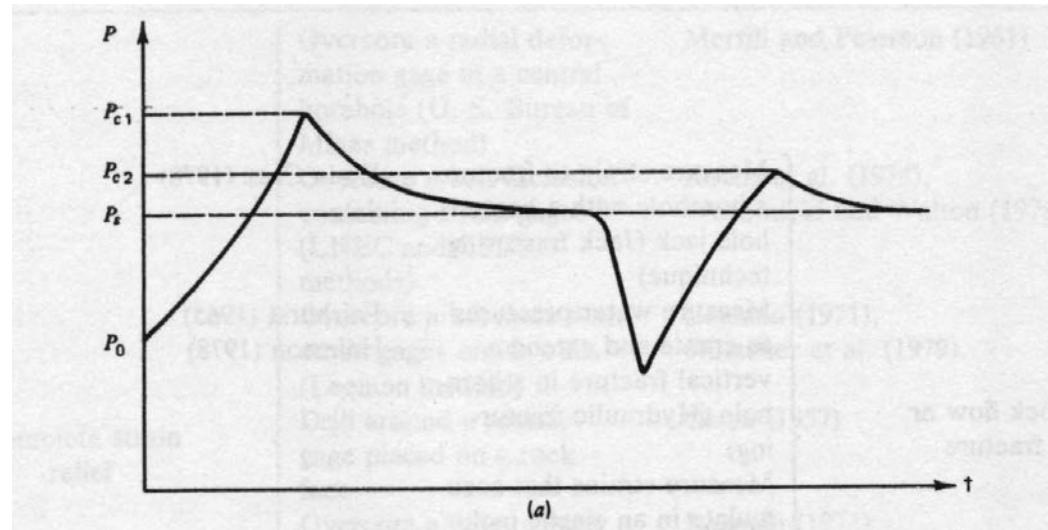
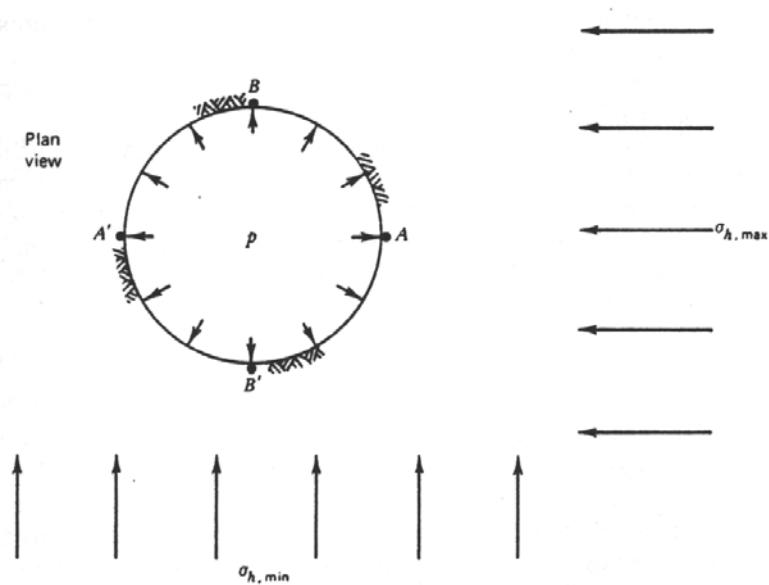
Hydraulic fracture

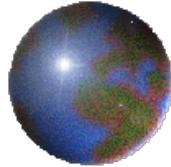




Hydraulic fracture

- P_s : shut-in pressure (steady value)
- P_{c1} : crack forming
- P_{c2} : crack opening





Hydraulic fracture

$$\sigma_\theta = \frac{\sigma_h + \sigma_v}{2} \cdot (1 + \frac{a^2}{r^2}) - \frac{\sigma_h - \sigma_v}{2} \cdot (1 + \frac{3 \cdot a^4}{r^4}) \cdot \cos 2\theta$$

P_s : shut-in pressure (steady value)

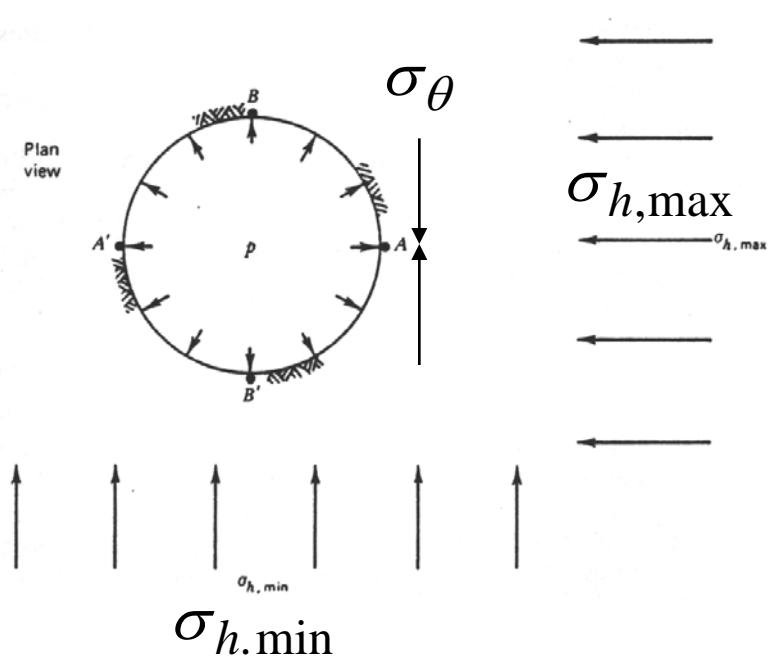
P_{c1} : crack forming

P_{c2} : crack opening

From Kirsch's solution

At point A and A' ($\theta=0, 180^\circ$)

$$\sigma_\theta = 3 \cdot \sigma_{h,\min} - \sigma_{h,\max}$$



1. Cracks occurs when pressure $p = P_{c1}$

$$P_{c1} - \sigma_\theta = T_o$$

$$P_{c1} - 3 \cdot \sigma_{h,\min} + \sigma_{h,\max} = T_o$$

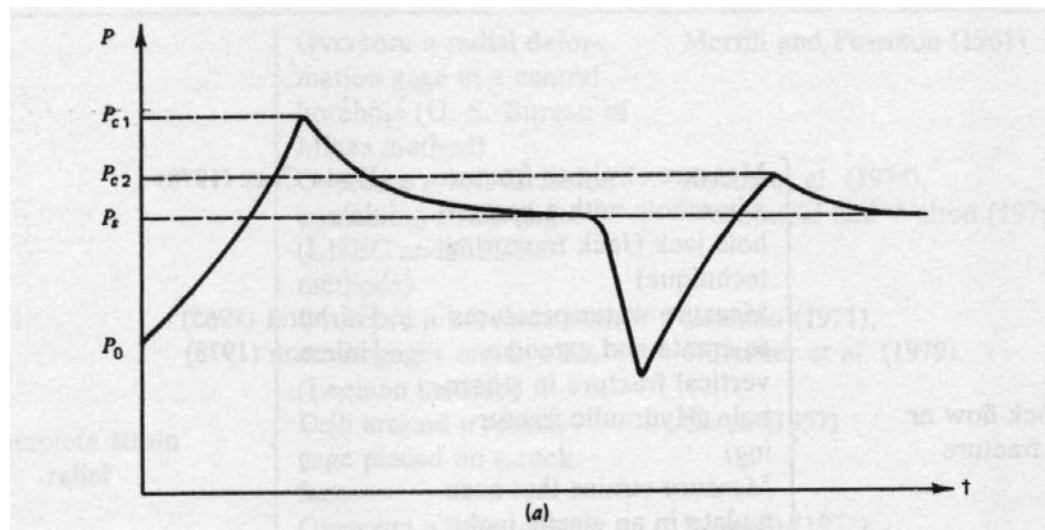
$$\sigma_{h,\max} = 3 \cdot \sigma_{h,\min} - P_{c1} + T_o$$

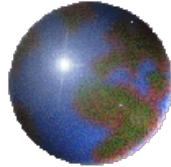
2. Cracks propagate when pressure $p = P_s$

$$P_s = \sigma_{h,\min}$$

$$T_o = ?$$

$$T_o = P_{c1} - P_{c2}$$





Hydraulic fracture

P_s : shut-in pressure (steady value)

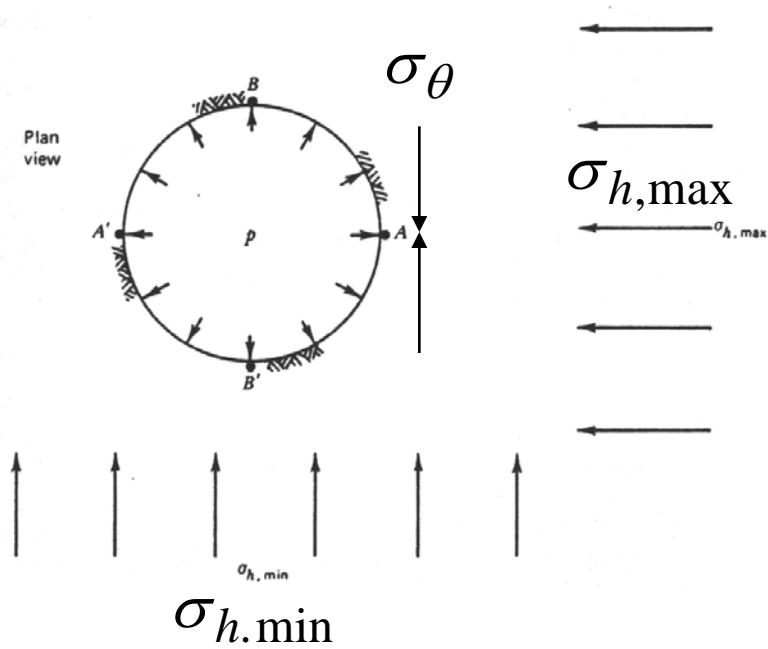
P_{c1} : crack forming

P_{c2} : crack opening

From Kirsch's solution

At point A and A' ($q=0,180$)

$$\sigma_\theta = 3 \cdot \sigma_{h,\min} - \sigma_{h,\max}$$



1. Cracks occurs when pressure $p = P_{c1}$

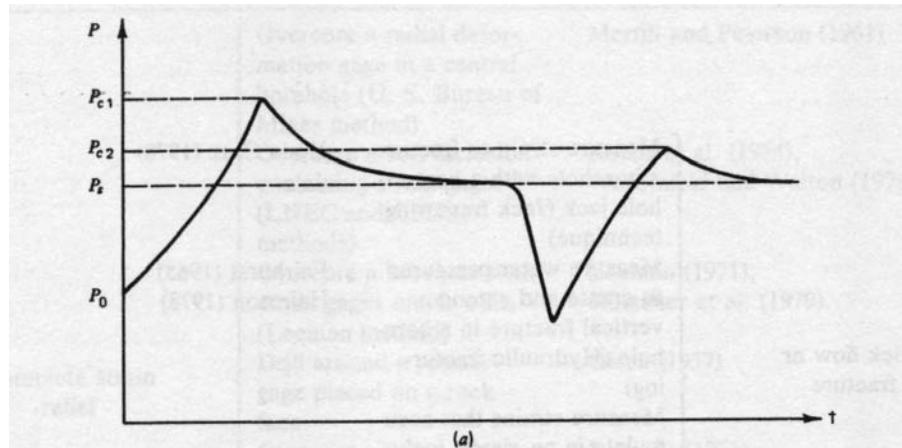
$$P_{c1} - \sigma_\theta = T_o$$

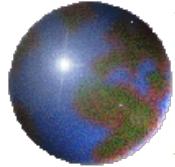
*If vertical stress is too small,
i.e. depth is too shallow*

$$P_{c1} - \sigma_v = T_o$$

*Horizontal fracture will occur,
You cannot find horizontal stress*

$$\sigma_v > (3 \cdot \frac{\sigma_{h,\min}}{\sigma_{h,\max}} - 1) \cdot \sigma_{h,\max} \quad (\sigma_v > \sigma_\theta)$$

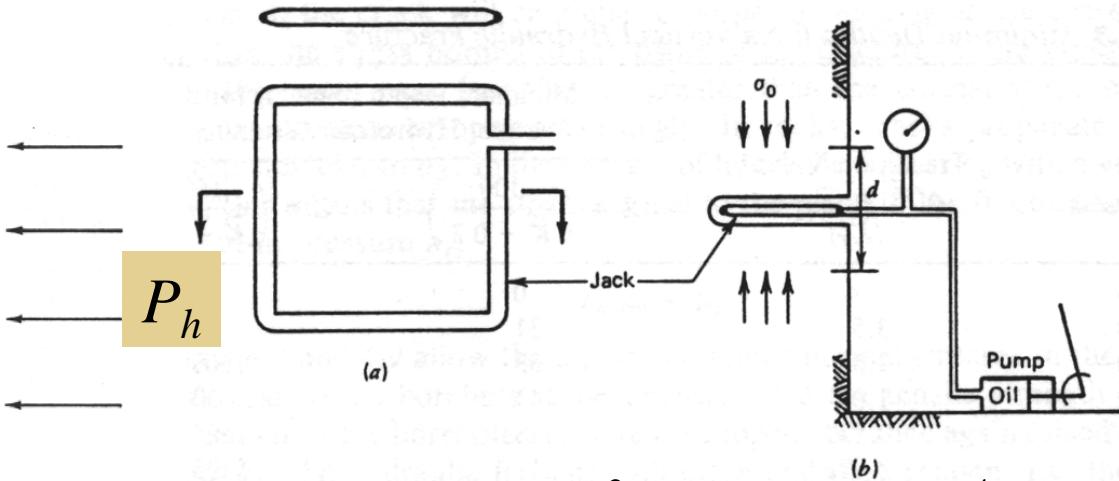
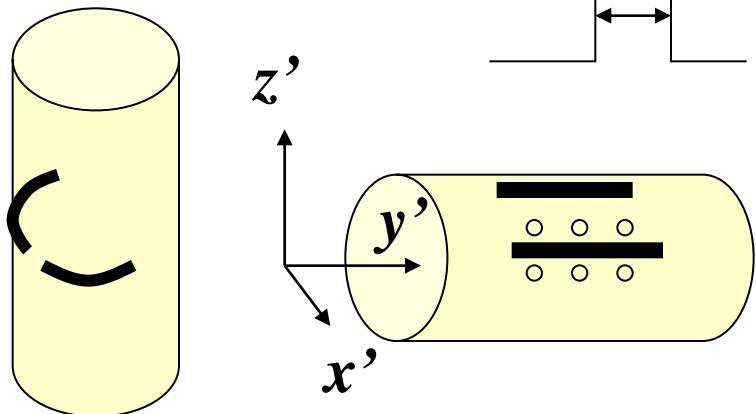
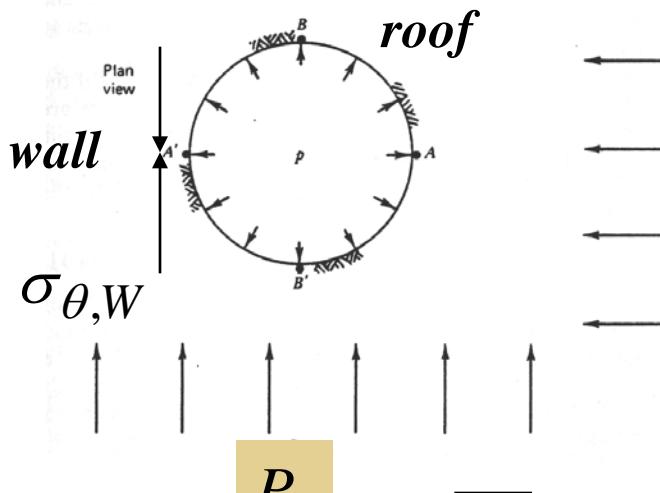




Flat jack method (measure compensate stress)

$$\sigma_{\theta,R} = 3 \cdot P_h - P_v$$

$$\sigma_{\theta,W} = 3 \cdot P_v - P_h$$



$$\sigma_\theta = \frac{\sigma_h + \sigma_v}{2} \cdot \left(1 + \frac{a^2}{r^2}\right) - \frac{\sigma_h - \sigma_v}{2} \cdot \left(1 + \frac{3 \cdot a^4}{r^4}\right) \cdot \cos 2\theta$$

